

What is the value of reliability?

Mogens Fosgerau

What is the value of travel time variability?

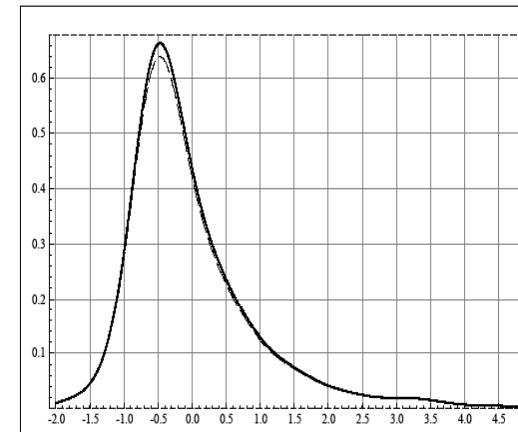
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Suggested terminology

- Travel time : TT
- Value of travel time : VTT
- Travel time variability : TTV
- Value of travel time variability : VTTV
 - Reliability is an unfortunate term
 - More appropriate for things that may break down, such as a service
 - The thing we are after is that travel times are inherently variable
 - Travel time variability is costly, hence “**value of travel time variability**”
 - Perhaps it would be even better to say cost of travel time and cost of travel time variability
 - I stay with VTT, VTTV

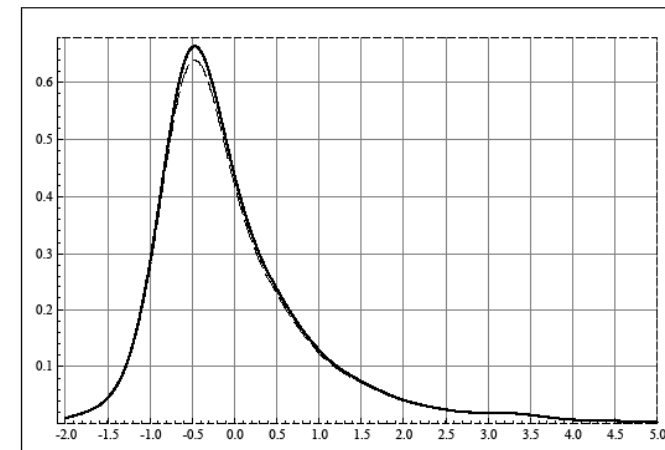
The value of what?

- VTT is the value of travel time
- Travel time is an unambiguous quantity, a number
- VTTV is the value of something else relating to a travel time distribution
- This is ambiguous!
- TT distributions can be described in many ways
- Examples from the literature :
 - Standard deviation, variance, 90% and other quantiles
- Other possibilities :
 - Interquartile range, skewness, kurtosis,
- In principle, all moments of the travel time distribution are relevant ...



How to choose a measure

- Depends on how travel times are actually distributed
- Depends on which kind of changes are relevant
- Depends on traveler preferences
- Employ standard neoclassical microeconomic framework
- Take travel time distribution as given
- Let's see what can be done with this



Theoretical framework

- Traveler chooses act : departure time
 - Consider travel by car – departure time can be freely chosen
 - Travel by scheduled service is another story
- "Nature" chooses travel time at random from travel time distribution **f**
- Outcome : departure time **dep**, arrival time **arr**

- Traveler knows all this
- He has rational preferences defined over outcomes
 - Utility function then exists
 - Embodies attitude to risk
 - Preferred choice maximizes expected utility
- Traveler acts (chooses optimal departure time **dep***) to maximize expected utility

How to derive VTTV from this?

- Consider

$$\mathbf{V}(\mathbf{f}) = \mathbf{EU}(\mathbf{dep}^*, \mathbf{dep}^* + \mathbf{travel\ time} \mid \mathbf{f})$$

- Travel time is random, follows \mathbf{f}
- Departure time \mathbf{dep}^* is optimal given \mathbf{f}
- Arrival time is random, $\mathbf{arr} = \mathbf{dep}^* + \mathbf{travel\ time}$
- VTTV is change in $\mathbf{V}(\mathbf{f})$ per unit change in \mathbf{f}
- What unit ... ?
 - We cannot say without making more assumptions
 - Necessary to consider special case

Scheduling preferences

- Use simple form based on Vickrey (1969), Small (1982)
- Assume there is a preferred arrival time **PAT**

$$U(\text{dep}, \text{arr}) = \alpha \cdot (\text{arr} - \text{dep}) + \beta \cdot (\text{arr} - \text{PAT})^- + \gamma \cdot (\text{arr} - \text{PAT})^+$$

- Function of travel time, earliness, lateness
- Building on Noland & Small (1995) and Bates et al (2001),
- Fosgerau & Karlström (2009) show that optimal expected utility has simple form, linear in mean and standard deviation of travel time
- Works for any travel time distribution
 - That has a mean

The VTTV according to Fosgerau & Karlström

- Under (α, β, γ) -preferences and typical neoclassical assumptions
- The optimal expected utility is

$$V(\mathbf{f}) = \alpha \cdot \text{mean} + (\beta + \gamma) \cdot H(\text{standardized } \mathbf{f}, \beta, \gamma) \cdot \text{stddev}$$

- And so the VTTV is $(\beta + \gamma) \cdot H(\text{standardized } \mathbf{f}, \beta, \gamma)$
- This can be estimated
- This can be translated from one \mathbf{f} to another since \mathbf{H} is known
- Works with standard deviation, quantiles, buffers or any other measure of scale

Vices and virtues of this definition of VTTV

Virtues

- This does what we want
- Measure of TTV is standard deviation
- VTTV can be derived from (α, β, γ)
- Depends on standardized travel time distribution in controlled way
- PAT does not appear (maxed out)
- Some robustness

Vices

- Very particular utility function
- Is (α, β, γ) a good description of preferences? Not necessarily
- VTTV depends on standardized travel time distribution, is it constant?
- Not additive across links in a network

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Measuring (α, β, γ)

- These parameters are of independent interest
 - Important for explaining congestion (Vickrey 1969, Arnott, de Palma, Lindsey 1993)
 - Can be used to derive the value of headway (Fosgerau 2009)
- Parameters can be measured in several ways
 - RP : from temporal shape of queues
 - SP : from choices between alternatives with different travel time distributions
 - a little bit more is needed to get (α, β, γ) and not just VTTV
 - SP : from scheduling choices

SP with travel time distributions

- SP alternatives comprising travel time distributions
 - E.g. 5 equally probable travel times
- A recent fashion
- I doubt the validity of the approach
 - Information overload, too much to digest
 - We know from behavioral economics that people have a hard time dealing with probabilities. There are systematic biases
- Safer to go for scheduling choices, not involving random travel time, provided we can make it work

Anomalies

- Systematic deviations from neoclassical rationality
- Anomalies are widespread and well documented
 - Mostly in lab, experiments, survey
 - Less in real life
- Loss aversion, probability weighting
 - Loss aversion tends to diminish with experience
- Our response depends on what we are doing
- Measurement of preferences :
 - necessary to account for anomalies, especially with SP!
- Prediction of behavior : depends...
- CBA : not clear that anomalies should be allowed into CBA
 - CBA framework is neoclassical
 - Distinction between choice and hedonic preferences

Some travel time distribution questions

- Are standardized travel time distributions reasonably stable across time and place?
- Can travel time distributions be predicted? It is not sufficient to consider just variance
- Can we generalize from links to network OD?

Conclusion

- Fosgerau & Karlström :
 - the standard deviation is a good measure of TTV
 - Consistent with (α, β, γ) -preferences
 - Sound basis in microeconomic theory
 - Works with any travel time distribution (essentially)
 - But VTTV still depends on standardized travel time distribution
- There may be better models
 - This is the best so far
- Lots of empirical work remains to be done
- Measurement of scheduling preferences
- Properties of travel time distributions